High spin band structure in ¹³⁹Nd^{*}

XU Qiang(徐强)¹⁾ ZHU Sheng-Jiang(朱胜江)^{1;1)} CHE Xing-Lai(车兴来)¹ DING Huai-Bo(丁怀博)¹ GU Long(顾龙)¹ ZHU Li-Hua(竺礼华)² WU Xiao-Guang(吴晓光)² LIU Ying(刘颖)² HE Chuang-Ye(贺创业)² LI Li-Hua(李立华)² PAN Bo(潘波)² HAO Xin(郝昕)² LI Guang-Sheng(李广生)²

1 (Department of Physics, Tsinghua University, Beijing 100084, China) 2 (China Institute of Atomic Energy, Beijing 102413, China)

Abstract High-spin states in ¹³⁹Nd nucleus have been reinvestigated with the reaction ¹²⁸Te (¹⁶O, 5n) at a beam energy of 90 MeV. The level scheme has been expanded with spin up to $47/2~\hbar$. At the low spin states, the yrast collective structure built on the $\nu h_{11/2}^{-1}$ multiplet shows a transitional shape with $\gamma \approx 32^{\circ}$ according to calculations of the triaxial rotor-plus-particle model. Three collective oblate bands with $\gamma \sim -60^{\circ}$ at the high spin states were identified for the first time. A band crossing is observed around $\hbar\omega \sim 0.4$ MeV in one oblate band based on the $25/2^-$ level.

Key words high-spin states, γ - γ coincidence, band crossing, oblate band

PACS 21.10.Re, 23.20.Lv, 27.60.+j

1 Introduction

The odd- A^{139} Nd nucleus with Z=60 and N=79lies in the transitional region with the neutron number approaching the closed shell at N=82. In this region, their level structures exhibit complex characteristics as existence of competition between the collective motion and the single-particle motion. At high spin states, as the proton Fermi surface lies near the bottom of the $\pi h_{11/2}$ subshell and the neutron Fermi surface lies near the top of the $\nu h_{11/2}$ subshell, the rotational alignment of a pair of protons from the lower $h_{11/2}$ midshell drives the nucleus to a near-prolate $(\gamma \sim 0^{\circ})$ shape while the rotational alignment of a pair of $h_{11/2}$ neutrons from the upper midshell drives the nucleus to an oblate shape $(\gamma \sim -60^{\circ})^{[1]}$ in the Lund convention^[2]. Thus, the different excitations of quasiparticles may drive a nucleus to form different shapes and sometimes shape coexistence may be observed in a nucleus^[3]. In previous publications, the high spin levels of many nuclei in this region, such as in ¹³⁷La^[4], $^{137}\text{Ce}^{[5]}$, $^{138}\text{Pr}^{[6]}$, $^{137}\text{Nd}^{[7]}$ and $^{140}\text{Nd}^{[8]}$, have been extensively researched. In the previous works on 139 Nd, some lower spin levels by using the $(^{16}\text{O}, 5\text{n})^{[9]}$ and $(\alpha, x\text{n})^{[10, 11]}$ reactions were reported. At very high spin states the triaxial superdeformed bands were observed through the $(^{48}\text{Ca}, 4\text{n})$ reaction $^{[12]}$. In this article, we report on experimental research on high-spin states and collective-band structures in 139 Nd in more detail. When this work was in progress, Kumar et al. $^{[13]}$ published some high-spin states in 139 Nd. Comparing with the results obtained in Ref. [13], we updated the high-spin scheme of 139 Nd. Some new levels and transitions have been identified, a collective band structure reported in Ref. [13] is rearranged, and so that the three new oblate bands have been newly observed.

2 Experiment and results

High spin states in ¹³⁹Nd were populated via the ¹²⁸Te(¹⁶O, 5n) fusion evaporation reaction at a beam energy of 90 MeV. An isotopically enriched ¹²⁸Te target of thickness 2.7 mg/cm² evaporated on a natural

Received 3 September 2008

^{*} Supported by National Natural Science Foundation of China (10575057, 10775078), Major State Basic Research Development Program (2007CB815005) and Special Program of Higher Education Science Foundation (20070003149)

 $^{1)\,}E\text{-mail:}\,zhushj@mail.tsinghua.edu.cn$

^{©2009} Chinese Physical Society and the Institute of High Energy Physics of the Chinese Academy of Sciences and the Institute of Modern Physics of the Chinese Academy of Sciences and IOP Publishing Ltd

aurum backing of 22 mg/cm² was bombarded by a beam of 16 O ions accelerated by the HI-13 accelerator at the China Institute of Atomic Energy (CIAE). An array of fourteen Compton-suppressed Ge detectors was employed to measure the in-beam γ -rays. The resolutions of the Ge detectors are between 1.8 and 2.2 keV at 1.333 MeV γ -ray energy. A γ - γ coincidence matrix was built, from which the γ - γ coincidence dada analysis was carried out. After subtracting background, about 5.8×10^7 efficient coincidence events were collected. The γ -ray energies and efficiencies were calibrated with 152 Eu source. To determine the multipolarity of γ -ray transitions, five detectors near 90° with respect to the beam axis were

sorted against the other nine detectors at 30°(three), 55° (one), 125° (one) and 150° (four) to produce a two dimensional angular correlation matrix from which it was possible to extract the average directional correlation of oriented state (DCO) intensity ratios. The γ - γ coincidence data were analyzed with the Radware software package^[14]. The level scheme of ¹³⁹Nd deduced from the present study is shown in Fig. 1. It was constructed from the γ - γ coincidence, the relative transition intensities, and DCO ratio analysis. The transition intensities are represented by the width of arrows. Collective bands and cascades newly observed are labeled on the top of the scheme.

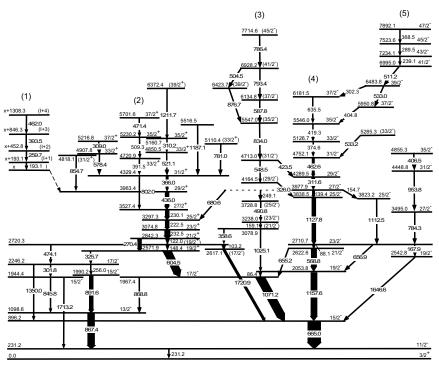


Fig. 1. Level scheme of 139 Nd.

3 Discussion

Shape transition is a very interesting phenomenon in $A{=}135$ transitional region. The prolate-oblate shape transition at the low spin states was reported in neighboring Ba^[15], Ce^[5, 16] and Nd^[9] isotopes between $N{=}77$ and $N{=}79$. That is, in a isotopic chain the nucleus has a prolate shape with $\gamma < 30^{\circ}$ at $N \leqslant 77$ and it has an oblate shape with $\gamma \geqslant 30^{\circ}$ at $N \leqslant 79$. It has indicated that the sequence of the $13/2^{-}$ and $15/2^{-}$ levels of the $\nu h_{11/2}^{-1}$ multiplet is a signature of a prolate or an oblate shape. When the $15/2^{-}$ state lies up on the $13/2^{-}$ state, the nucleus has a prolate shape, whereas when the level inversion of the $13/2^{-}$ state and $15/2^{-}$ state occurs, the nucleus

has an oblate shape. In order to further understand the structural characteristics at the low spin states in $^{139}{\rm Nd}$, we have performed calculations using the triaxial rotor-plus-particle model with a variable moment of inertia (VMI)^{[17-19]}. In the calculations, the adjustable parameters are $\varepsilon_2,\,\gamma$ and Coriolis attenuation factor $\chi.$ By varying the $\varepsilon_2,\,\gamma$ and χ values, and by carefully comparing the calculated levels with the corresponding experimental ones, we determined these values used in the calculations as follows: $\varepsilon_2=0.11,\,\varepsilon_4=0.04,\,\gamma=31.6^\circ$ and $\chi=0.76.$ Other parameters were taken as standard. The results of our calculations and a comparison with experimental data are shown in Fig. 2. Generally, the agreement between the theoretical and experimental results is good. In

the calculations, the levels are very sensitive to the parameters γ and χ , but not to ε_2 and ε_4 . When we fixed other parameters, and changed the γ value from 0° to 45° , the levels varied with the γ value, as shown in Fig. 3. It indicates that the level inversion of $13/2^-$ state and $15/2^-$ state occurs around $\gamma = 31.6^{\circ}$. The best agreement between calculational and experimental energy levels happens at $\gamma = 31.6^{\circ}$. The prolate-oblate shape transition at the low spin states in the Nd isotopes indeed occurs between N=77 and N=79.

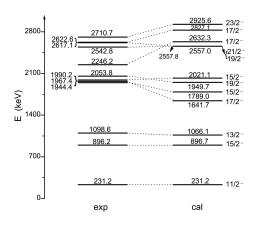


Fig. 2. Calculated levels of some members of the $\nu h_{11/2}^{-1}$ and comparison to the experiment for the ¹³⁹Nd.

The most interesting finding of the present study is the collective bands (1), (4) and (5). These three bands show similar features to the other known oblate bands in the $A \sim 130$ region: (a) much stronger $\Delta I = 1$ transitions relative to the $\Delta I = 2$ transitions inside the band, (b) no signature splitting occurring, and (c) different moments of inertia $(J^{(1)})$ from those of prolate bands. Plots of the moments of inertia $(J^{(1)})$ of the collective bands (1), (2) and (3) in ¹³⁹Nd along with the oblate bands in ¹³⁷Ce^[5], ¹³⁸Ce^[20], ¹³⁵La^[21], and ¹³⁶La^[22] against the rotational frequency $\hbar \omega$ are shown in Fig. 4. One can see that the $J^{(1)}$ of the

bands (1), (4) and (5) in 139 Nd show similar behavior to the oblate bands in the neighboring nuclei. Examining the band (4), we can see a backbending (band crossing) of band (4) occurs around at $\hbar\omega \sim 0.4$ MeV. This band crossing may be caused by the alignment of a pair of protons, as the first alignment of a pair of neutron has happened to drive the nucleus to form the oblate shape at this band head level. The reason for this band crossing still needs to be confirmed by further works.

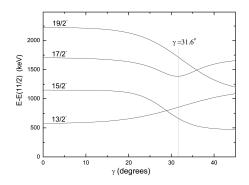


Fig. 3. The calculated some levels with γ value in 139 Nd. The vertical line indicates the experiment data. The energies of $11/2^-$ levels are taken as zero.

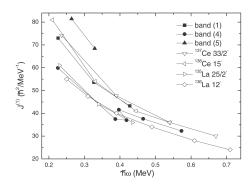


Fig. 4. Comparison of the moments of inertia $(J^{(1)})$ of bands (1), (4) and (5) in 139 Nd with the oblate bands in 137 Ce, 138 Ce, 135 La, 136 La and the prolate bands in 135 Ce.

References

- 1 Paul E S et al. Phys. Rev. Lett., 1987, 58: 984
- 2 Andersson G et al. Nucl. Phys. A, 1976, 268: 205
- 3 Paul E S et al. Phys. Rev. C, 1989, 40: 1255
- 4 LI M L et al. Eur. Phys. J. A, 2006, 28: 1
- 5 ZHU S J et al. Phys. Rev. C, 2000, **62**: 044310
- 6 LI M L et al. Phys. Rev. C, 2007, 75: 034304
- 7 Petrache C M et al. Nucl. Phys. A, 1997, **617**: 228
- 8 Petrache C M et al. Phys. Rev. C, 2005, **72**: 064318
- 9 Gizon J et al. J. Phys. G, 1978, 4: L171
- 10~ Ludziejewski J et al. Z. Phys. A, 1977, ${\bf 281}:~287$
- 11 Muller-Veggian M et al. Nucl. Phys. A, 1980, **344**: 89

- 12 Petrache C M et al. Phys. Rev. C, 2000, **61**: 011305
- 13~ Kumar S et al. Phys. Rev. C, 2007, ${\bf 76} \colon 014306$
- 14 Radford D C. Nucl. Instrum. Methods Phys. Res., Sect. A, 1995, 361: 297
- 15 CHE X L et al. Eur. Phys. J. A, 2006, 30: 347
- 16~ Kortelahti M et al. Phys. Scr., 1983, ${\bf 27}:~166$
- 17 XING Z et al. HEP & NP, 1996, 20: 85 (in Chinese)
- 18 ZHU S J et al. Chin. Phys. Lett., 1998, 15: 793
- 19 Sakhaee M et al. Phys. Rev. C, 1999, **60**: 067303
- 20 ZHU S J et al. Chin. Phys. Lett., 1999, 16: 635
- 21 MA R et al. Phys. Rev. C, 1990, 41: 2624
- 22 ZHU S J et al. Eur. Phys. J. A, 2005, ${\bf 24}$: 199