

Towards the decays of $\bar{N}_X(1625)$ in the molecular picture*

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Abstract In this talk, we firstly overview the experimental status of $\bar{N}_X(1625)$, which is an enhancement structure observed in $K^-\bar{\Lambda}$ invariant mass spectrum of $J/\psi \rightarrow pK^-\bar{\Lambda}$ process. Then we present the result of the decay of $\bar{N}_X(1625)$ under the two molecular assumptions, i.e. S -wave $\bar{\Lambda}K^-$ and S -wave $\bar{\Sigma}^0K^-$ molecular states. Several experimental suggestions for $\bar{N}_X(1625)$ are proposed.

Key words molecular state, strong decay, rescattering mechanism

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1 Introduction

J/ψ decay is an ideal platform for studying the excited baryons and hyperons. With the collected data, the BES experiment has carried out a series of investigations of hadron spectroscopy. Among the new observations of the hadron states, $\bar{N}_X(1625)$ is an enhancement near $K^-\bar{\Lambda}$ threshold, which was only reported in several conference proceedings^[1–3] under the investigation of $K^-\bar{\Lambda}$ invariant mass spectrum in $J/\psi \rightarrow pK^-\bar{\Lambda}$ process. The rough measurement results about the mass and the width of $\bar{N}_X(1625)$ are $m = 1500\text{--}1650$ MeV and $\Gamma = 70\text{--}110$ MeV, respectively. The experiment also indicates that the spin-

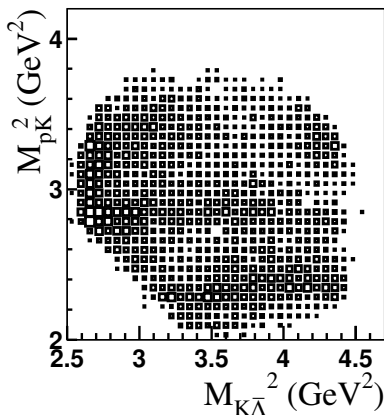


Fig. 1. The Dalitz plot of $J/\psi \rightarrow pK^-\bar{\Lambda}$ in Ref. [3].

parity favors $\frac{1}{2}^-$ for $\bar{N}_X(1625)$, which denotes the antiparticle of $\bar{N}_X(1625)$ ^[3]. The $pK^-\bar{\Lambda}$ Dalitz plot and $K^-\bar{\Lambda}$ invariant mass spectrum are shown in Figs. 1 and 2. $\bar{N}_X(1625)$ enhancement structure was not observed in $\gamma p \rightarrow K^+\Lambda$ process at SAPHIR^[4].

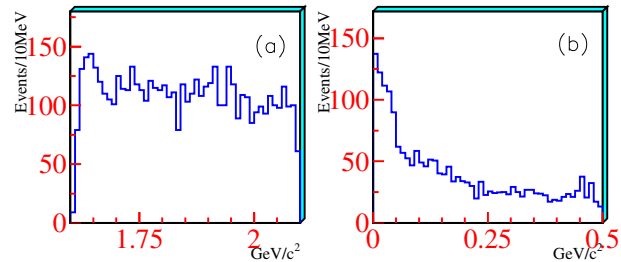


Fig. 2. The invariant mass spectrum (a) $M_{K^-\bar{\Lambda}}$ from $J/\psi \rightarrow pK^-\bar{\Lambda}$ and (b) the $M_{K^-\bar{\Lambda}} - M_{K^-\bar{\Sigma}}$ after the efficiency and phase space correction from Ref. [3].

At Hadron 07 conference, the BES Collaboration reported the preliminary new experiment result of $\bar{N}_X(1625)$. Its mass and width are well determined as^[5]

$$m = 1625_{-7-23}^{+5+13} \text{ MeV}, \quad \Gamma = 43_{-7-11}^{+10+28} \text{ MeV},$$

respectively. The production rate of $\bar{N}_X(1625)$ is

$$B[J/\psi \rightarrow p\bar{N}_X(1625)] \cdot B[\bar{N}_X(1625) \rightarrow K^-\bar{\Lambda}] = (9.14_{-1.25-8.28}^{+1.30+4.24}) \times 10^{-5}.$$

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These more accurate experimental information of $\bar{N}_X(1625)$ provides us good chance to study the nature of $\bar{N}_X(1625)$.

If $\bar{N}_X(1625)$ is a regular baryon, the branching ratio of $J/\psi \rightarrow p\bar{N}_X(1625)$ should be comparable with that of $J/\psi \rightarrow p\bar{p}$ considering the branching ratio $B(J/\psi \rightarrow p\bar{p}) = 2.17 \times 10^{-3}$ ^[6]. Thus, we can obtain $B[\bar{N}_X(1625) \rightarrow \bar{\Lambda}K^-] \sim 10\%$, which indicates that there exists the strong coupling between $\bar{N}_X(1625)$ and $K^-\bar{\Lambda}$.

This peculiar property of $\bar{N}_X(1625)$ inspires our interest in exploring its structure, especially in its exotic component. In Ref. [7], we calculated the possible decay modes of $\bar{N}_X(1625)$ in the two different assumptions of the molecular states, i.e. $\bar{\Lambda}-K^-$ and $\bar{\Sigma}^0-K^-$. In the following, we will present the details of the calculation and the numerical result.

2 The decays under the assumptions of $\bar{\Lambda}-K^-$ and $\bar{\Sigma}^0-K^-$ molecular states

Since the mass of $\bar{N}_X(1625)$ is above the threshold of $\bar{\Lambda}$ and K^- under the assumptions of $\bar{\Lambda}-K^-$ molecular state, thus $\bar{N}_X(1625)$ can directly decay into $\bar{\Lambda}+K^-$ (Fig. 3 (a)), which is depicted by the decay amplitude

$$\mathcal{M}[\bar{N}_X(1625) \rightarrow \bar{\Lambda}+K^-] = i\mathcal{G}\bar{v}_N\gamma_5 v_{\bar{\Lambda}}. \quad (1)$$

Here \mathcal{G} denotes the coupling constant between $\bar{N}_X(1625)$ and $\bar{\Lambda}K^-$. $v_{\bar{\Lambda}}$ and v_N are the spinors.

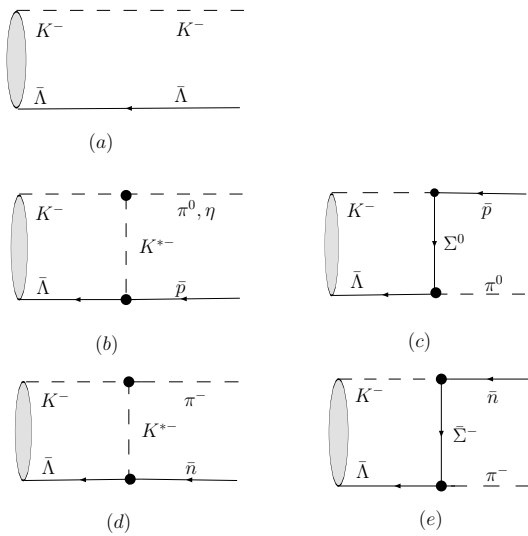


Fig. 3. The decay modes if $\bar{N}_X(1625)$ is $\bar{\Lambda}-K^-$ molecular state.

In the rescattering mechanism, the subordinate decays $\bar{N}_X(1625) \rightarrow \pi^0\bar{p}$, $\eta\bar{p}$, $\pi^-\bar{n}$ occur, which are

depicted in Fig. 3(c)—(e). The effective Lagrangians relevant to the calculation are^[8, 9]:

$$\mathcal{L}_{\mathcal{P}\mathcal{P}\mathcal{V}} = -ig_{\mathcal{P}\mathcal{P}\mathcal{V}}\text{Tr}([\mathcal{P}, \partial_\mu \mathcal{P}]\mathcal{V}^\mu), \quad (2)$$

$$\mathcal{L}_{\mathcal{B}\mathcal{B}\mathcal{P}} = F_P\text{Tr}(\mathcal{P}[\mathcal{B}, \bar{\mathcal{B}}])\gamma_5 + D_P\text{Tr}(\mathcal{P}\{\mathcal{B}, \bar{\mathcal{B}}\})\gamma_5, \quad (3)$$

$$\mathcal{L}_{\mathcal{B}\mathcal{B}\mathcal{V}} = F_V\text{Tr}(\mathcal{V}^\mu[\mathcal{B}, \bar{\mathcal{B}}])\gamma_\mu + D_V\text{Tr}(\mathcal{V}^\mu\{\mathcal{B}, \bar{\mathcal{B}}\})\gamma_\mu, \quad (4)$$

where $\bar{\mathcal{B}}$ is the Hermitian conjugate of \mathcal{B} . \mathcal{P} , \mathcal{V} and \mathcal{B} respectively denote the octet pseudoscalar meson, the nonet vector meson and the baryon matrices. F_P and D_P in Eq. (3) and F_V and D_V in Eq. (4) satisfy the relations $F_P/D_P = 0.6$ ^[10] and $F_V/(F_V + D_V) = 1$ ^[11]. In the limit of $SU(3)$ symmetry, by $g_{NN\pi} = 13.5$ and $g_{NN\rho} = 3.25$ ^[12], one obtains the meson-baryon coupling constants relevant to our calculation: $g_{\mathcal{P}\mathcal{P}\mathcal{V}} = 6.1$, $F_P = 13.5$, $D_P = 0$, $F_V = 1.2$, $D_V = 2.0$.

Since the intermediate states $\bar{\Lambda}$ and K^- in Fig. 3(b)—(d) are on-shell, one writes out the general amplitude expression corresponding to Fig. 3 (b) and (d) by Cutkosky cutting rules

$$\begin{aligned} \mathcal{M}_1^{(\mathcal{A}_1, c_1)} &= \frac{1}{2} \int \frac{d^3 p_1}{(2\pi)^3 2E_1} \frac{d^3 p_2}{(2\pi)^3 2E_2} \times \\ &(2\pi)^4 \delta^4(M_N - p_1 - p_2) [i\mathcal{G}\bar{v}_N\gamma_5 v_{\bar{\Lambda}}] \times \\ &[ig_1 \bar{v}_{\bar{\Lambda}}\gamma_\mu v_{\mathcal{A}_1}] [ig_2 (p_1 + p_3)_\nu] \frac{i}{q^2 - M_{\mathcal{C}_1}^2} \times \\ &\left[-g^{\mu\nu} + \frac{q^\mu q^\nu}{M_{\mathcal{C}_1}^2} \right] \mathcal{F}^2(M_{\mathcal{C}_1}, q^2). \end{aligned} \quad (5)$$

For Fig. 3(c) and (e), the general amplitude expression is

$$\begin{aligned} \mathcal{M}_1^{(\mathcal{A}_2, c_2)} &= \frac{1}{2} \int \frac{d^3 p_1}{(2\pi)^3 2E_1} \frac{d^3 p_2}{(2\pi)^3 2E_2} \times \\ &(2\pi)^4 \delta^4(M_N - p_1 - p_2) [i\mathcal{G}\bar{v}_N\gamma_5 v_{\bar{\Lambda}}] \times \\ &[ig'_2 \bar{v}_{\bar{\Lambda}}\gamma_5] \frac{i(q + M_{\mathcal{C}_2})}{q^2 - M_{\mathcal{C}_2}^2} [ig'_1 \gamma_5 v_{\mathcal{A}_2}] \times \\ &\mathcal{F}^2(M_{\mathcal{C}_2}, q^2). \end{aligned} \quad (6)$$

In the above expressions, \mathcal{C}_i and \mathcal{A}_i denote the exchanged particle and the final state baryon, respectively. p_1 and p_2 are respectively the four momenta of K^- and $\bar{\Lambda}$. $\mathcal{F}^2(m_i, q^2)$ denotes the form factor which compensates the off-shell effects of the hadrons at the vertices. In this work, one takes $\mathcal{F}^2(m_i, q^2)$ as the monopole form^[13, 14] $\mathcal{F}^2(m_i, q^2) = \left(\frac{\xi^2 - m_i^2}{\xi^2 - q^2} \right)^2$, which plays the role to cut off the end effect. Phenomenological parameter ξ is parameterized as $\xi = m_i + \alpha\Lambda_{\text{QCD}}$, where m_i denotes the mass of exchanged meson^[15]

and $\Lambda_{\text{QCD}} = 220$ MeV. α is a phenomenological parameter and is of order unity.

In the $\bar{\Sigma}^0 - K^-$ molecular picture, $\bar{N}_X(1625)$ does not decay into $\bar{\Sigma}^0$ and K^- because of having not enough phase space. However, decay $\bar{N}_X(1625) \rightarrow \bar{\Lambda} + K^-$ occurs by the isospin violation effect, which results in the mixing of Σ^0 with Λ ^[15] (Fig. 4 (a)). By the Lagrangian

$$\mathcal{L}_{\text{mixing}} = g_{\text{mixing}}(\bar{\psi}_{\Sigma^0}\psi_{\Lambda} + \bar{\psi}_{\Lambda}\psi_{\Sigma^0}),$$

with the coupling constant $g_{\text{mixing}} = 0.5 \pm 0.1$ MeV determined by QCD sum rule^[15], one writes out the decay amplitude

$$\mathcal{M}[\bar{N}_X(1625) \rightarrow \bar{\Sigma}^0 + K^-] = \mathcal{G} g_{\text{mixing}} \bar{v}_N \gamma_5 \frac{i}{\not{p} - M_{\Lambda}} v_{\bar{\Lambda}}, \quad (7)$$

where p and M_{Λ} are the four momentum and the mass of $\bar{\Lambda}$, respectively.

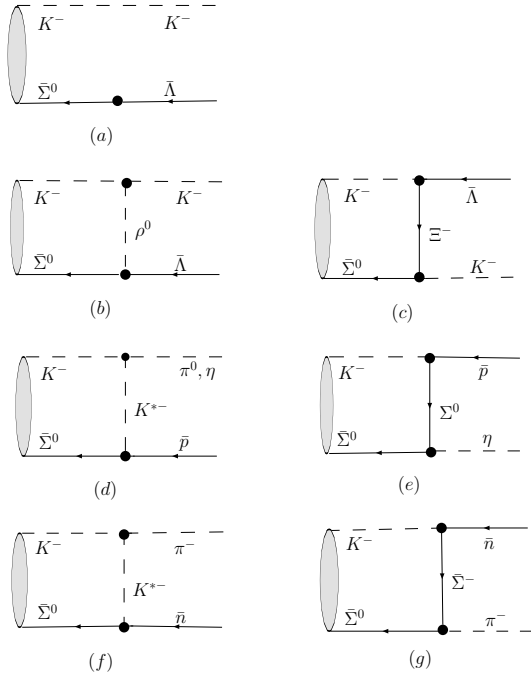


Fig. 4. The decay modes if $\bar{N}_X(1625)$ is $\bar{\Sigma}^0 - K^-$ molecular state.

For $\bar{\Sigma}^0 - K^-$ molecular state assumption, $\bar{N}_X(1625)$ still can decay into $\pi^0 \bar{p}$, $\eta \bar{p}$, $\pi^- \bar{n}$, which are described in Fig. 4(b)–(g). The general expression of Fig. 4(b), (d), (f) is expressed as

$$\mathcal{M}_3^{(A_3, C_3)} = \int \frac{d^4 q}{(2\pi)^4} [i\mathcal{G} \bar{v}_N \gamma_5] \frac{i}{-\not{p}_2 - M_{\Sigma^0}} [ig_3 \gamma_\mu v_{A_3}] \times [ig_4 (p_1 + p_3)_\nu] \frac{-ig^{\mu\nu}}{q^2 - M_{C_3}^2} \frac{i}{p_1^2 - M_K^2} \times \mathcal{F}^2(M_{C_3}, q^2), \quad (8)$$

for Fig. 4(c), (e), (g) the general amplitude expression reads as

$$\mathcal{M}_4^{(A_4, C_4)} = \int \frac{d^4 q}{(2\pi)^4} [i\mathcal{G} \bar{v}_N \gamma_5] \frac{i(\not{p}_2 - M_{\Sigma^0})}{-p_2^2 - M_{\Sigma^0}^2} [ig_4' \gamma_5] \times \frac{i(q + M_{C_4})}{q^2 - M_{C_4}^2} [ig_3' \gamma_5 v_{A_4}] \times \frac{i}{p_1^2 - M_K^2} \mathcal{F}^2(M_{C_4}, q^2), \quad (9)$$

where p_1 and p_2 denote the four momenta carried by K^- and $\bar{\Sigma}^0$, respectively. $q = p_1 - p_3 = p_4 - p_2$. For the decays depicted in Fig. 4(b)–(g), $\bar{\Sigma}^0$ and K^- are off-shell. The form factor may provide a convergent behavior for the triangle loop integration, which is very similar to the case of the Pauli-Villars renormalization scheme^[16–18].

3 Numerical result

In Figs. 5 and 6, we show the ratios of the decay widths of $\bar{N}_X(1625) \rightarrow \pi^0 \bar{p}$, $\eta \bar{p}$, $\pi^- \bar{n}$ to the decay width of $\bar{N}_X(1625) \rightarrow \bar{\Lambda} K^-$ under the assumptions of $\bar{\Lambda} - K^-$ and $\bar{\Sigma}^0 - K^-$ molecular states when taking $\alpha = 1-3$. Fig. 5 and Fig. 6 illustrate that these ratios do not strongly depend on the α . One further obtains the typical values of these ratios taking $\alpha = 1.5$, which are listed in Table 1. Combining these ratios shown in Figs. 5 and 6 with the branching ratio $B[J/\psi \rightarrow p \bar{N}_X(1625)] \cdot B[\bar{N}_X(1625) \rightarrow K^- \bar{\Lambda}] = (9.14_{-1.25-8.28}^{+1.30+4.24}) \times 10^{-5}$ given by BES^[5], one estimates the branching ratio of the subordinate decays of $J/\psi \rightarrow p \bar{N}_X(1625) \rightarrow p(\pi^0 \bar{p})$, $p(\eta \bar{p})$, $p(\pi^- \bar{n})$, which are shown in Table 2.

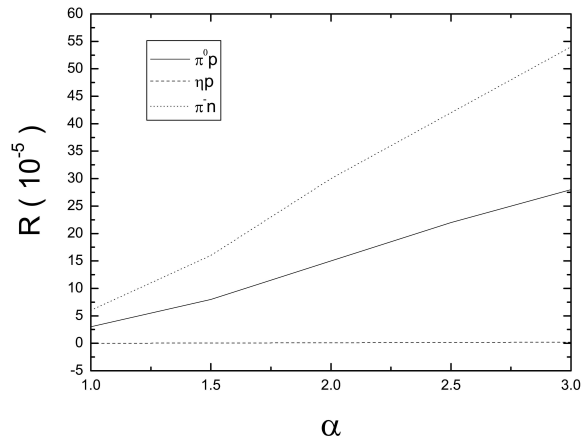


Fig. 5. The ratios of $\bar{N}_X(1625) \rightarrow \pi^0 \bar{p}, \eta \bar{p}, \pi^- \bar{n}$ decay widths to $\bar{N}_X(1625) \rightarrow \bar{\Lambda} K^-$ decay width under the assumption of $\bar{\Lambda} - K^-$ molecular state.

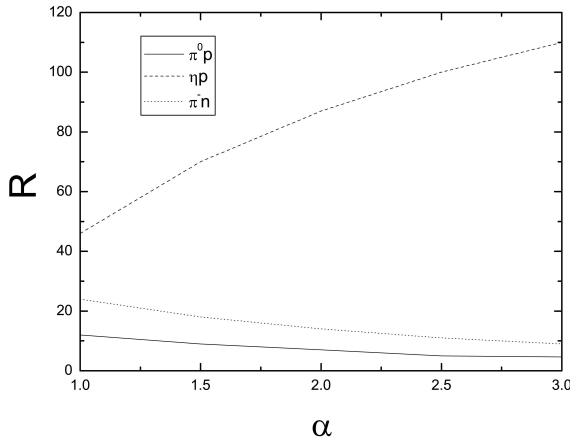


Fig. 6. The ratios of $\bar{N}_X(1625) \rightarrow \pi^0 \bar{p}, \eta \bar{p}, \pi^- \bar{n}$ decay widths to $\bar{N}_X(1625) \rightarrow \bar{\Lambda} K^-$ decay width in $\bar{\Sigma}^0 - K^-$ molecular state picture.

Table 1. The ratios of the decay widths of $\bar{N}_X(1625) \rightarrow \pi^0 \bar{p}, \eta \bar{p}, \pi^- \bar{n}$ to the decay width of $\bar{N}_X(1625) \rightarrow \bar{\Lambda} K^-$ in different molecular assumptions with $\alpha = 1.5$.

	$\frac{\Gamma(\pi^0 \bar{p})}{\Gamma(K^- \bar{\Lambda})}$	$\frac{\Gamma(\eta \bar{p})}{\Gamma(K^- \bar{\Lambda})}$	$\frac{\Gamma(\pi^- \bar{n})}{\Gamma(K^- \bar{\Lambda})}$
$\bar{\Lambda} - K^-$	1×10^{-4}	5×10^{-7}	2×10^{-4}
$\bar{\Sigma}^0 - K^-$	9	70	18

4 Discussion and conclusion

Assuming $\bar{N}_X(1625)$ as $\bar{\Lambda} - K^-$ molecular state, $K^- \bar{\Lambda}$ is the dominant decay mode of $\bar{N}_X(1625)$. The branching ratio of $\bar{N}_X(1625) \rightarrow K^- \bar{\Lambda}$ is far larger than the branching ratios of $\bar{N}_X(1625) \rightarrow \pi^0 \bar{p}, \eta \bar{p}, \pi^- \bar{n}$, which can explain why $\bar{N}_X(1625)$ was firstly observed in the mass spectrum of $K^- \bar{\Lambda}$. And we notice that the smallest measurable branching ratio for J/ψ decay listed in the Particle Data Book^[6] is about 10^{-5} .

Thus, it is difficult to measure $J/\psi \rightarrow p \bar{N}_X(1625) \rightarrow p(\pi^0 \bar{p}), p(\eta \bar{p}), p(\pi^- \bar{n})$ in further experiments.

Under the assumption of S -wave $\bar{\Sigma}^0 - K^-$ molecular state for $\bar{N}_X(1625)$, $\bar{N}_X(1625)$ can not decay to $\bar{\Sigma}^0 K^-$ due to having not enough phase space. The $\Lambda - \Sigma^0$ mixing mechanism and final state interaction effect result in the decay $\bar{N}_X(1625) \rightarrow \bar{\Lambda} K^-$. The branching ratio of $\bar{N}_X(1625) \rightarrow \bar{\Lambda} K^-$ is about one or two order smaller than that of $\bar{N}_X(1625) \rightarrow \pi^0 \bar{p}, \eta \bar{p}, \pi^- \bar{n}$. The sum of the branching ratios of $\bar{N}_X(1625) \rightarrow \pi^0 \bar{p}, \eta \bar{p}, \pi^- \bar{n}$ listed in Table 2 is about 10^{-2} . Such a large branching ratio is unreasonable for J/ψ decay. The BES collaboration has already studied $J/\psi \rightarrow p \pi^- \bar{n}$ in Ref. [19] and $J/\psi \rightarrow p(\eta \bar{p})$ in Ref. [20]. The branching ratios respectively corresponding to $J/\psi \rightarrow p \pi^- \bar{n}$ and $J/\psi \rightarrow p \eta \bar{p}$ are 2.4×10^{-3} and 2.1×10^{-3} ^[19, 20]. Although these experimental values are comparable with our numerical result of the corresponding channel, the former experiments did not find the structure consistent with $\bar{N}_X(1625)$, which seems to show that the evidence against S -wave $\bar{\Sigma}^0 - K^-$ molecular picture is gradually accumulating^[7].

As indicated in Ref. [5], there exists very strong coupling between $\bar{N}_X(1625)$ and $\bar{\Lambda} K^-$. At present other decay modes of $\bar{N}_X(1625)$ are still missing^[5]. Thus the assumption of S -wave $\bar{\Lambda} - K^-$ molecular state is more favorable than that of S -wave $\bar{\Sigma}^0 - K^-$ molecular state for $\bar{N}_X(1625)$. The result of Ref. [21], which is from the calculation within the framework of the chiral $SU(3)$ quark model by solving a resonating group method (RGM) equation, indicates that the ΛK system is unbound. Whether there exists the S -wave $\bar{\Lambda} - K^-$ molecular state is still an open issue. The dynamics study of S -wave $\bar{\Lambda} - K^-$ system by other phenomenological models is encouraged.

Table 2. The branching ratios of $J/\psi \rightarrow p \bar{N}_X(1625) \rightarrow p(\pi^0 \bar{p}), p(\eta \bar{p}), p(\pi^- \bar{n})$ in two different molecular state pictures for $\bar{N}_X(1625)$.

	$\bar{\Lambda} - K^-$ system	$\bar{\Sigma}^0 - K^-$ system
$J/\psi \rightarrow p \bar{N}_X(1625) \rightarrow p(\pi^0 \bar{p})$	$1 \times 10^{-8} \sim 3 \times 10^{-8}$	$\sim 1 \times 10^{-3}$
$J/\psi \rightarrow p \bar{N}_X(1625) \rightarrow p(\eta \bar{p})$	$4 \times 10^{-11} \sim 2 \times 10^{-10}$	$\sim 7 \times 10^{-3}$
$J/\psi \rightarrow p \bar{N}_X(1625) \rightarrow p(\pi^- \bar{n})$	$2 \times 10^{-8} \sim 5 \times 10^{-8}$	$\sim 2 \times 10^{-3}$

If it is problematic to explain $\bar{N}_X(1625)$ as the pure molecular state structure, we have to again ask what is the underlying structure of $\bar{N}_X(1625)$. We notice that there exist two well established states $N^*(1535)$ and $N^*(1650)$ with $J^P = 1/2^-$ nearby the mass of $N_X(1625)$. In PDG^[6], the branching ratio of

$N^*(1650) \rightarrow K \Lambda$ is about 3%—11%. The authors of Ref. [22] indicated that $N^*(1535)$ should have large $s\bar{s}$ component in its wave function which shows the large $N^*(1535)K\Lambda$ coupling. $N^*(1535)$ and $N^*(1650)$ can strongly couple to $K\Lambda$. Thus, whether $N_X(1625)$ enhancement is related to $N^*(1535)$ and $N^*(1650)$ is

also an interesting topic.

Finally, we want to propose several suggestions for future experiment:

Until now, the experimental information of $\bar{N}_X(1625)$ only appeared in the proceeding of conference^[1–3, 5]. We are expecting the formal publication of this enhancement, which will be helpful to stimulate more experimentalists and theorists to pay attention to this issue.

Searching for $\bar{N}_X(1625) \rightarrow \pi^0 \bar{p}, \eta \bar{p}, \pi^- \bar{n}$ modes in future experiment can shed light on the nature of $\bar{N}_X(1625)$. We urge our experimental colleague carefully analyze $J/\psi \rightarrow \pi \pi^- \bar{n}$ and $J/\psi \rightarrow \pi \eta \bar{p}$ channel in further experiments, especially in the forthcoming

BESIII.

Confirming $\bar{N}_X(1625)$ by the other experiments is encouraged. At present, Lanzhou CSR is a good platform to study the baryon spectroscopy. Analyzing the invariant mass spectrum of $K^+ \Lambda$, which comes from the $p\alpha$ reaction, will be an important approach to investigate the $N_X(1625)$ enhancement structure.

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